# Baldivis Secondary College



### Semester Two Examination, 2017

### Question/Answer booklet

# MATHEMATICS

**SOLUTIONS**

**METHODS**

**UNITS 3 AND 4**

## Section One:

## Calculator-free

|  |  |  |  |  |  |  |  |  |  |  |
| --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- |
| Student Number: In figures |  |  |  |  |  |  |  |  |  |  |

In words

Your name

## Time allowed for this section

Reading time before commencing work: five minutes

Working time: fifty minutes

## Materials required/recommended for this section

***To be provided by the supervisor***

This Question/Answer booklet

Formula sheet

***To be provided by the candidate***

Standard items: pens (blue/black preferred), pencils (including coloured), sharpener, correction fluid/tape, eraser, ruler, highlighters

Special items: nil

## Important note to candidates

No other items may be taken into the examination room. It is **your** responsibility to ensure that you do not have any unauthorised material. If you have any unauthorised material with you, hand it to the supervisor **before** reading any further.

## Structure of this paper

|  |  |  |  |  |  |
| --- | --- | --- | --- | --- | --- |
| Section | Number of questions available | Number of questions to be answered | Working  time (minutes) | Marks available | Percentage of examination |
| Section One:  Calculator-free | 8 | 8 | 50 | 52 | 35 |
| Section Two:  Calculator-assumed | 13 | 13 | 100 | 97 | 65 |
|  | | |  | **Total** | 100 |

## Instructions to candidates

1. The rules for the conduct of examinations are detailed in the school handbook. Sitting this examination implies that you agree to abide by these rules.

2. Write your answers in this Question/Answer booklet.

3. You must be careful to confine your response to the specific question asked and to follow any instructions that are specified to a particular question.

4. Additional working space pages at the end of this Question/Answer booklet are for planning or continuing an answer. If you use these pages, indicate at the original answer, the page number it is planned/continued on and write the question number being planned/continued on the additional working space page.

5. Show all your working clearly. Your working should be in sufficient detail to allow your answers to be checked readily and for marks to be awarded for reasoning. Incorrect answers given without supporting reasoning cannot be allocated any marks. For any question or part question worth more than two marks, valid working or justification is required to receive full marks. If you repeat any question, ensure that you cancel the answer you do not wish to have marked.

6. It is recommended that you do not use pencil, except in diagrams.

7. The Formula sheet is not to be handed in with your Question/Answer booklet.

Section One: Calculator-free 35% (52 Marks)

This section has**eight (****8)** questions. Answer **all** questions. Write your answers in the spaces provided.

Working time: 50 minutes.

Question 1 (6 marks)

The discrete random variable is defined by

(a) Determine the value of the constant . (2 marks)

|  |
| --- |
| **Solution** |
|  |
| **Specific behaviours** |
| ✓ sums probabilities to 1  ✓ states value |

(b) Determine

(i) . (2 marks)

|  |
| --- |
| **Solution** |
| Bernoulli distribution, |
| **Specific behaviours** |
| ✓ uses  ✓ determines expected value |

(ii) . (2 marks)

|  |
| --- |
| **Solution** |
|  |
| **Specific behaviours** |
| ✓ uses  ✓ determines required variance |

Question 2 (6 marks)

(a) Determine , if . (3 marks)

|  |
| --- |
| **Solution** |
|  |
| **Specific behaviours** |
| ✓ writes as  ✓ writes as  ✓ combines as single log and states value of |

(b) Determine the exact solution to . (3 marks)

|  |
| --- |
| **Alternative solution** |
|  |
| **Specific behaviours** |
| ✓ divides both sides by 3  ✓ logs to base 4  ✓ solves for |

|  |
| --- |
| **Solution** |
|  |
| **Specific behaviours** |
| ✓ divides both sides by 3  ✓ logs both sides to any base  ✓ solves for |

Question 3 (7 marks)

The rate of change of displacement of a particle moving in a straight line at any time seconds is given by

Initially, when , the particle is at , a fixed point on the line.

(a) Calculate the initial velocity of the particle. (1 mark)

|  |
| --- |
| **Solution** |
|  |
| **Specific behaviours** |
| ✓ velocity |

(b) Determine the distance of the particle from after seconds. (3 marks)

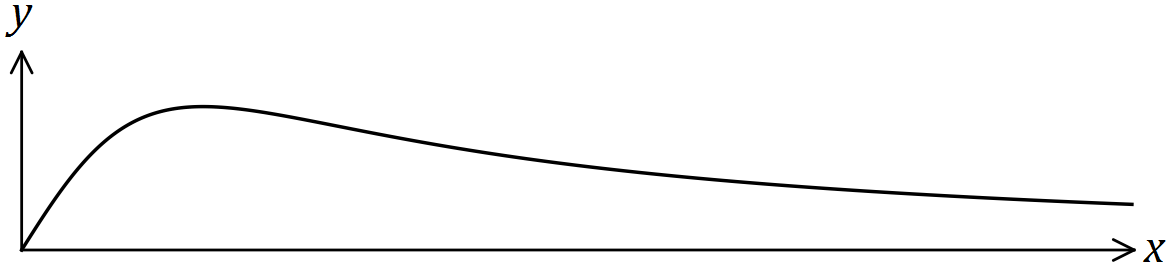
|  |
| --- |
| **Solution** |
|  |
| **Specific behaviours** |
| ✓ integrates  ✓ evaluates constant  ✓ substitutes to obtain distance |

(c) Determine when the acceleration of the particle is . (3 marks)

|  |
| --- |
| **Solution** |
|  |
| **Specific behaviours** |
| ✓ differentiates for acceleration  ✓ eliminates  ✓ solves for |

Question 4 (7 marks)

The graph of , is shown below, where .



(a) Determine the gradient of the curve when . (3 marks)

|  |
| --- |
| **Solution** |
|  |
| **Specific behaviours** |
| ✓ uses quotient rule  ✓ correct  ✓ correct gradient |

(b) Determine the exact area bounded by the curve and the lines and , simplifying your answer. (4 marks)

|  |
| --- |
| **Solution** |
|  |
| **Specific behaviours** |
| ✓ writes integral  ✓ antidifferentiates  ✓ substitutes  ✓ simplifies |

Question 5 (6 marks)

The functions and intersect at the point .

The first derivatives of the functions are and .

Determine an expression for each function.

|  |
| --- |
| **Solution** |
|  |
| **Specific behaviours** |
| ✓ antidifferentiates  ✓ evaluates constant  ✓ states in simplified form  ✓ antidifferentiates  ✓ evaluates constant  ✓ states in simplified form |

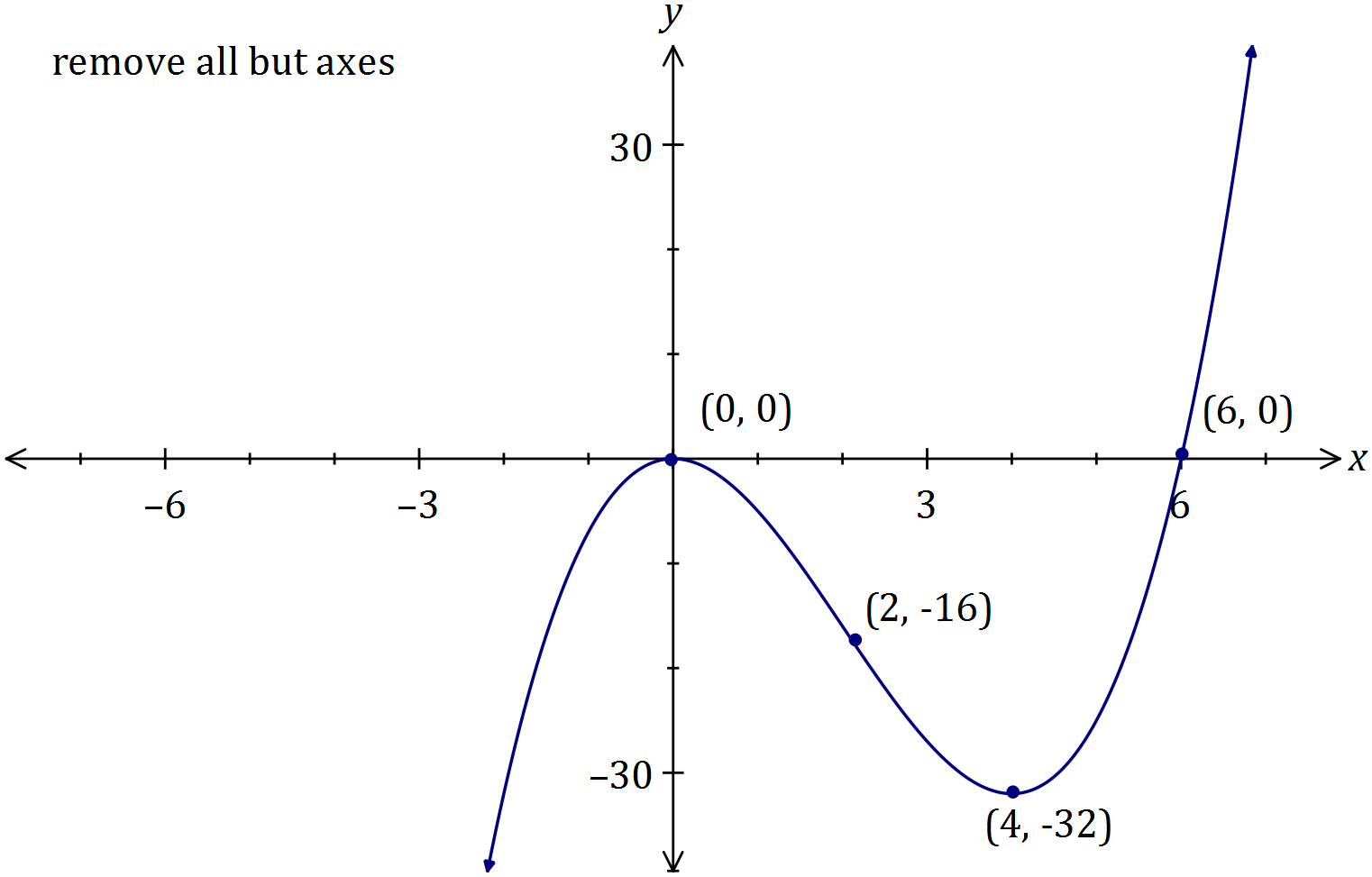
Question 6 (8 marks)

A curve has first derivative and passes through the point .

(a) Determine the value(s) of for which . (2 marks)

|  |
| --- |
| **Solution** |
|  |
| **Specific behaviours** |
| ✓ differentiates  ✓ states value |

(b) Sketch the curve on the axes below, clearly indicating the location of all axes intercepts, stationary points and points of inflection. (6 marks)



|  |
| --- |
| **Solution** |
|  |
| **Specific behaviours** |
| ✓ obtains expression for  ✓ obtains zeroes of  ✓ indicates coordinates of minimum and point of inflection  ✓ indicates scale  ✓ indicates location on graph of min, max, pt infl, roots  ✓ single smooth continuous curve |

Question 7 (7 marks)

A function is defined by .

(a) State the natural domain of . (1 mark)

|  |
| --- |
| **Solution** |
|  |
| **Specific behaviours** |
| ✓ states domain |

(b) Show that . (3 marks)

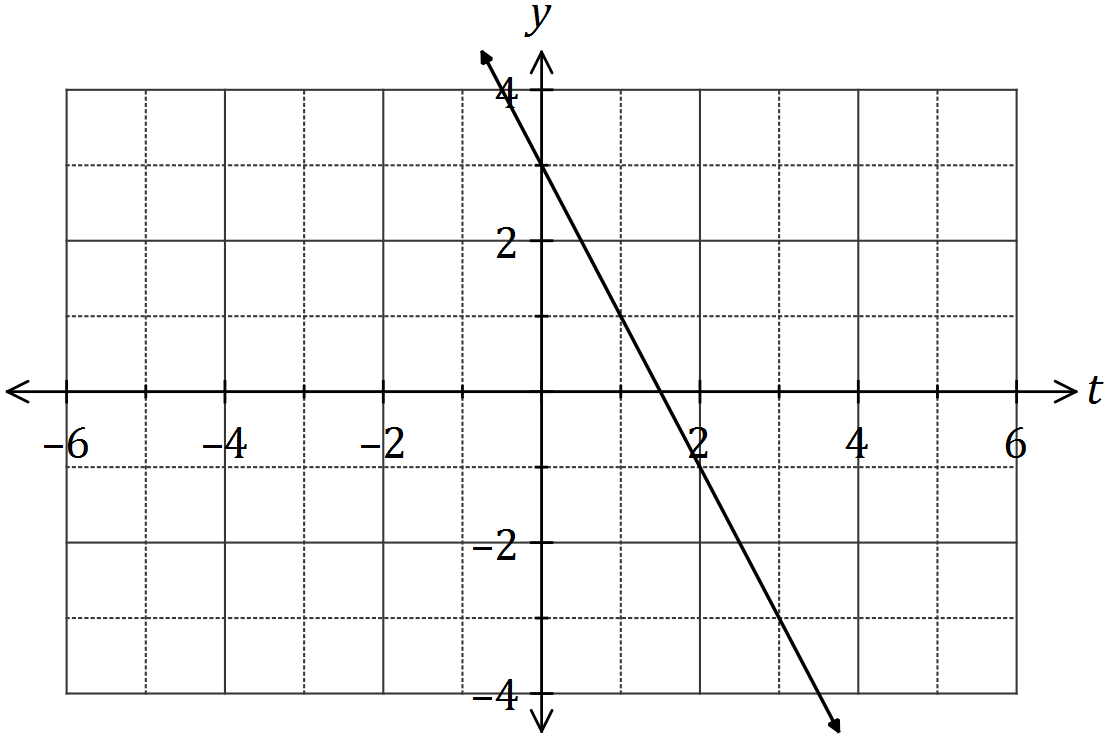
|  |
| --- |
| **Solution** |
|  |
| **Specific behaviours** |
| ✓ uses quotient rule  ✓ and expressions  ✓ substitutes , showing numerator is |

(c) Use the second derivative test to determine the nature of the stationary point of the function at . (3 marks)

|  |
| --- |
| **Solution** |
|  |
| **Specific behaviours** |
| ✓ simplifies and differentiates with quotient rule  ✓ differentiates correctly  ✓ indicates and interprets sign of |

Question 8 (5 marks)

Part of the graph of the linear function is shown below.



Another function is given by

Use the increments formula to estimate the change in as increases from to .

|  |
| --- |
| **Solution** |
|  |
| **Specific behaviours** |
| ✓ indicates  ✓ uses  ✓ determines  ✓ uses increments formula  ✓ determines change |

Additional working space

Question number: \_\_\_\_\_\_\_\_\_

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